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'9AGKA;8&05:;9KJ;=9&A5G&*9=@9AB&"::6:;A5;=&&&&&&I*.6&2DD`&_W*R*7,&2DDG& 9.-:607-,;&\$'&Q-0R-.-+=&U+%7&P#*0"#=&Q-0R-.-+& Z\$0,#60.&Q-0R-.-+&P6.,60&

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- "W77-7,+.,&8.7,0*",\$0&'\$0&'\$0&'\$06&'\$*076&+.)&6YK60-6.,-+%6)*"+,-\$.&''\$*076c&+77-7,6)&-.&''\$*076b)67-R.=&6:+%+,6)&7,*)6.,&K60'\$0<+.''6=&K0\$:-)6)&1+"bR0\$*.)&-.'\$0<+,-\$.&,#0\$*R#&%6'',*067& +.)&)-7"*77-\$.7&\$'&''\$*076&06+)-.R7M&&
- 5\$0b6)&M-,#&'+''*%;&+.)&7,+''&\$.&)6:6%K<6.,&+.)&+)<-.-7,0+,-\$.&-77*67&'\$0&+&*.-:607-,;&K<6.,&+.)&+)<-.-7,0+,-\$.&-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...)&+,-\$...,A-77*67&'\$0&+&*.-:607-,;&K<6.,&+...,A-70*,;K-70*,

>+&S0+)=&IN&g&/;)6=&WN&AFC2`EN&BT(W!V&W&h*+%,+,-:6&B.i*-0;&.,\$&S0\$j6'',HX+76)&>6+0.-.R=& FFAFEN& &

>+&S0+)=&IN&AFC23EN&^#6&P\$+%,-\$. &\$'&(776.,-+%!''#\$\$%7&+.)&*0+%()*''+,-\$.+&\6'\$0<N&

/;)6=&WN&g&>+&S0+)=&IN&AFC23EN&4-.)'*% 677=&T6<\$"0+";=&+.)&()*"+,-\$.N&

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>+&S0+)=&IN=&4-.b=&WN&g&]m!,66.=&XN&FCCCFC23EVPP@\$X7,HP!@\$X7,KDy`RA@PPT@PPD@PabD!@UBP0P&501417.931-6

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 $>+\&S0+)=\&IIA\&>^{*}.7<+..=\&PIAU$77=\&^N&J$)M-.=\&JAA!6+&&IIA&G&n-&'#=&4N&AFCC`EN&qS&+..,-.R&!66)7&'$0&(.R+R6)&>6+0.-.RNr&&^#6&P$+&,-$.&$'&(776.,-+&!''#$$7m&U+&WU$0^{*}<=&W&S0-.''-K&6)&!,+.)=&Z$:6<160&GH2C=&FCC`=&^#6&W)+<m7&4+0&A'$,6&&T6.:60=&P$$$0+)$N&&A'$$

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 $>+\&SO+)=\&IN\&q(YK\&SO6=\&PO6+, 6=\&/+0:67,=\&] M. V&W. \&(YK60-6.,-+\&WKK0$+''#&, &&SO$'677-$.+\& T6:6\%$K<6., Nr&AFCC`EN&^#6&Z+,-$.+&!$''-6,;&'$0&(YK60-6.,-+&()*''+,-$.&AZ!((E&B?,#&W...*+&P$.'606.''6=&]'',$160&B2H&Z$:6<160&F=&FCC`=&!#60+,$.&/$,6&&!6+,,&G&=5+7#-.R,$.N& >+&SO+)=&IN=&S*,<+.=&TN=&A-, 60=&SN=&Q&5-&+<7=&AAFCC?EN&q^#-.b-.R&X6;$.)&,#6&P&+770$$<V&X*-&D-.R&+.)&^0+.7'$0<-.R&P$</p>$

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>+&S0+)=&IN&AFCC?EN&q4\$0+%()*"+,-\$.&+.)&,#6&4\$0+%]0)60&&&].6&/-R#&!"#\$\$%\r&^#6& 8.,60.+,-\$.+%P\$.'606."6&\$.&P-:-"&()*"+,-\$.V&\676+0"#&+.)&S0+",-"6=&I+.*+0;&2DHF2=&FCC?=& /-%\$.&/\$,6&&]0&.)\$IW%+<\$.,6&!K0-.R7=&U%\$0-)+N&

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>+&S0+)=&IN&AFCC?EN&qS%+.,-.R&!66)7&,\$&8.,6R0+,-.R&!60:-"6&>6+0.-.R&.&,#6&P*00-"*%*<Nr&^#6& 8.,60.+,-\$.+&P\$.'606."6&\$.&P-:-"&()*"+,-\$.V&\676+0"#&+.)&S0+",-"6=&I+.*+0;&2DHF2=&FCC?=& /-%\$.&/\$,6&&]0&.)\$IW%+<\$.,6&!K0-.R7=&U&\$0-)+N&&

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>+&S0+)=&IN&AFCC@EN&qW06&\$*0&K*1%''&7''#\$\$%7&''6.,607&'\$0&7\$''-+%j*7,-''6o=r&W<60-''+.&()*''+,-\$.+% !,*)-67&W77\$''-+,-\$.=&Z\$:6<160&FCC@=&d+.7+7&P-,;=&4-77\$*0-N&&

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>+&S0+)=&IN&AFCCFENqP\$<<*.-,;=&P\$.'%'',&+.)&.)-''606.''6V&^#6&4\$0+%+.)&(,#-''+%&77*67&\$'&+.& W<60-''+.&/-R#&!''#\$\$%FXW<60-''+.&()*''+,-\$.+%!,*)-67&W77\$''-+,-\$.=&Z\$:6<160&FCCF=& S-,,71*0R#=&S6..7;%+.-+N&

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>+&S0+)=&IN&AFCC2EN&q5#+,&>677\$.7&+06&^#6; &\6+%; &>6+0.-. Ro&W&!,*); &\$'&!,*)6., H^6+''#60& 8.,60+'',-\$.7&M-,#&S\$%''-67&+.)&P\$)67&\$'&/\$.\$0&.&+&P\$.,6<K\$0+0; &S*1%''&/-R#&!''#\$\$%r&W<60-''+.&()*''+,-\$.+&!,*)-67&W77\$''-+,-\$.=&Z\$:6<160&FCC2=&4-+<-=&U%\$0-)+N&

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>+&S0+)=&IN&AFCC2EN&q^#6&!\$"-+&U\$*.)+,-\$.7&\$'&P+06V&8<K%"+,-\$.7&'\$0&()*"+,-\$.=r&^#6& P#+0%\$,,67:-%6&P\$.'606.''6&\$.&(,#-''7&g&>6+)607#-K=&]'',\$160&FCC2=&P#+0%\$,,67:-%6=&Q-0R-.-+N&& &

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 $>+\&S0+)=\&IN\&A2DDGEN\&q5\#+,\&7\&.\ \&,\#6\&(YK60-6.\ "6V\&\&N\&>\$b\&+,\&P\$<<`*.-,;\&!60:-"6\&>6+0.-.\ R\&'0$<&+\&!$"-+&HS7; "\#$\%R-"+\%>6+0.-.\ R\&S607K6",-:6=r\&N<60-"+.\&()*"+,-$.+\&!,*)-67\&W77$"+,-$.=&Z$:6<160\&2DDG=\&S\#-\&+).6\%K\#-+&S6..7;&+.-+N\&$

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>+&S0+)=&IN&g&\+M%=&!N&FC2?EN&q\6)*"-.R&\6"-)-:-7<r&.:-,6)&)-+%\$R-"+%M\$0b7#\$K7&M-,#& 8.<+,67&+,&,#6&/6.0;&PN&/-%&P\$006",-\$.+%U+"-%,;m7&\66.,0;&!*<<-,=&J+%671*0R=&%.\$-7&.& 06K0676.,+,-\$.&\$'&589m7&

>+&S0+)=&IN&AFC22EN&e\6:-7-,-.R&I\$#.&T6M6;m7&

>+&\$0+)=&IN&AFCCDEN&q(YK%\$0-. R&,#6&! \$*,#60. &\$\$:60,; &>+M&P6. ,60f7&4 *%-<6)-+&.-,-+,-:6Nr& =&4+; &2D&H&FC=&FCCD=&!K\$\$. &\-:60&P\$%6R6=&4+''\$<1=&>N& e&+. & .: -, 6) & 6", *06&, \$&, #6&

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>+&S0+)=&IN=&U066.=&XN&g&/\$*%6=&dN&AFCC`EN&qS%+.,-.R&!66)7&\$0&P\$<<*.-,;&(.R+R6<6.,=r&U\$*0,#&W..*+&(.:-0\$.<6.,+&!*<<-,=&WK0-%2`=&FCC`=&9.-:607-,;&9.-\$.=&567,60.&&%.\$-7&9.-:607-,;&9.-\$.=&567,60.&&%.\$-7&9.-:607-,;&9.-\$.=&567,60.&&%.\$-7&9.-:607-,;&9.-\$.=&567,60.&&%.\$-7&9.-:607-,;&9.-\$.=&567,60.&&%.\$-7&9.-:607-,;&9.-\$.=&567,60.&&%.\$-7&60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.57,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,;&8.567,60.&&%.\$-7&607-,&8.567,60.&&%.\$-7&607-,&8.567,60.&&%.\$-8&607-,&8&607-,&8&607-,&8&607-&&8&60

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>+&S0+)=&IN&g&S*,<+.=&TN&AFCC`EN&q(YK60-6."-.R&,#6&("#\$67V&S\$)"+7,-.R&+.)&()*"+,-\$.=r& P](/!&(-R#,#&W..*+%A^6+"#&U67,=&4+0"#&F2=&FCC`=&/\$00+1-.&/+%&567,60.&&%.\$-7&9.-:607-,;N&&& &

>+&S0+)=&IN&AFCC3EN&qP\$..6",-\$.7&H&X6'\$06&+.)&W',60V&].&&<K%6<6.,-.R&,#6&J-0\$*Y&P#+%6.R6=r&2F,#&T6+%.R&M-,#&T-''606.''6&&.7,-,*,6=&!6K,6<160&2@H2`=&FCC3=&9.-:607-,;&9.-\$.=&567,60.& %%.\$-7&9.-:607-,;&

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 $>+\&S0+)=\&IN\&AFCC3EN\&q] . 6\&6) *''+, $0m7\&,0+. 7'$0<+,-$. \&-., $\&16''$<-. R\&+\&''#+. R6\&+R6., \&-. \&+\&K^*1\%''\& 7''#$$%&6.:-0$. <6., =r\&J0+.) &P\%+770$$<I(''#$&>6+0.-. Rm7\&! *<<60\&>6+0.-. R&8.7,-,*,6=&I*\% &DH 2@=&FCC3=&J0+.) &P+.; $. &+.) &U\%+R7,+''=&W0-a$. +N&&&$

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>+&S0+)=&IN&AFCC3EN&q].&J0\$*K&I\$*0.+%.R=r&J0+.)&P%+770\$\$<I(''#\$&>6+0.-.Rm7&!*<<60&>6+0.-.R&8.7,-,*,6=&I*%&DH2@=&FCC3=&J0+.)&P+.;\$.&+.)&U%+R7,+''=&W0-a\$.+N&&

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>+&S0+)=&IN&FCC@EN&qW06&\$*0&K*1%''&7''#\$\$%7&''6.,607&'\$0&!\$''-+&I*7,-''6or&589&P+<K*7&T-+&FR*6& .\$\$.H#\$*0&K0\$R0+<=&WK0-%2`=&FCC@=&9.-:607-,;&W0,&J+%60;=& -

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 $!"\#\$\%+07\#-K\$P\$<<-,,66\&<6<160\&4!"\#\$\$\%\&\$'\&()*"+,-\$.E=\&!K0-.R\&FCFC\&_\&S0676.,\&$

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 $\label{eq:constraint} \begin{array}{l} \mbox{\ } * \ , 00-"+.\ 6\&7\%+.\)\&] * \ , M+0)\&X\$*.\)\&! "\#\$\$\% \\ Z+,-\$.\ +\%(*0+\%()*"+,-\$.\ &W77\$"-+,-\$.\ \&\\ Z+,-\$.\ +\%!\ \$"-6,; \&\$`\&(YK60-6.\ ,-+\%()*"+,-\$.\ \&\\ Z\$0,\#\&P+0\$\%.\ +\&] * \ , M+0)\&X\$*.\)\&! "\#\$\$\% \\ [\] \mbox{\ } \#\$P+0\$\%.\ +\&] * \ , M+0)\&X\$*.\)\&! "\#\$\$\% \\ [\] \mbox{\ } \#\$Q+\%6; \&S\#-\%57\%K\#; \&\$`\&()*"+,-\$.\ \&!\ \$"-6,; \&$

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